

The supermesh

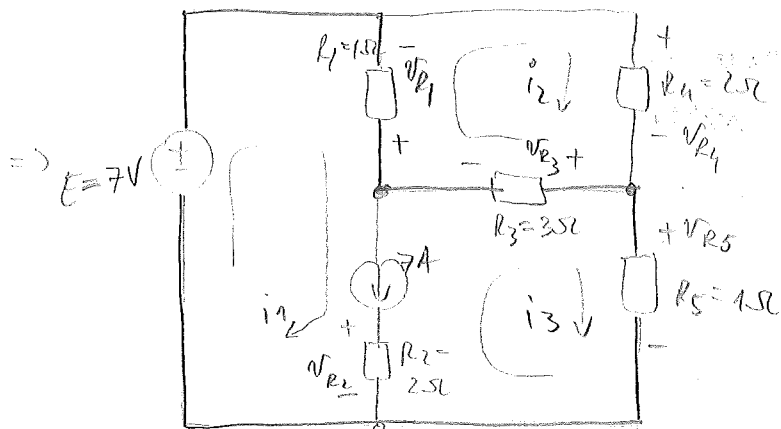
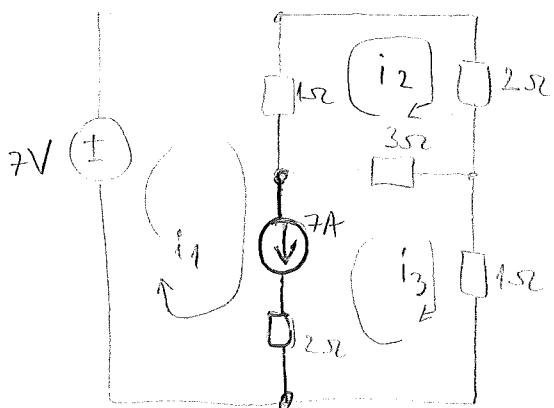
Note: Forget last time: (3) lots of statistics in production!

similar to the "supernode" technique from nodal analysis.

- Kec creates super-mesh from meshes that have a current source in common; with the current source in the interior of the supermesh.

- # of meshes is reduced by one.

Example:



loop i_1 + loop i_3 = supermesh.

Apply KLV for remaining loop(s) and supermesh:

$$\text{loop } (i_2): \begin{cases} v_{R_1} + v_{R_4} + v_{R_3} = 0 & \rightarrow R_1(i_2 - i_1) + R_4 i_2 + R_3(i_2 - i_3) = 0 \end{cases}$$

$$\text{supermesh } (i_1, i_3): \begin{cases} E + v_{R_1} + v_{R_3} = v_{R_5} & \rightarrow E + R_1(i_2 - i_1) + R_3(i_2 - i_3) = R_5 i_3 \end{cases}$$

$$\Rightarrow \begin{cases} \underbrace{i_2 - i_1} + \underbrace{2i_2} + \underbrace{3(i_2 - i_3)} = 0 \\ \underbrace{i_2 - i_1} + \underbrace{3(i_2 - i_3)} - i_3 = -7 \end{cases} \Rightarrow \begin{cases} -i_1 + 6i_2 - 3i_3 = 0 \\ -i_1 + 4i_2 - 4i_3 = -7 \end{cases}$$

Add also: (for the independent source).
 $7A = i_1 - i_3$
 3 equations
 3 unknowns.

$$\Rightarrow \begin{cases} i_1 - 6i_2 + 3i_3 = 0 \\ i_1 - 4i_2 + 4i_3 = 7 \\ i_1 - i_3 = 7 \end{cases} \Rightarrow A = \begin{bmatrix} 1 & -6 & 3 \\ 1 & -4 & 4 \\ 1 & 0 & -1 \end{bmatrix}, X = \begin{bmatrix} i_1 \\ i_2 \\ i_3 \end{bmatrix}, b = \begin{bmatrix} 0 \\ 7 \\ 7 \end{bmatrix}$$

$$\Rightarrow \boxed{AX = b} \rightarrow \text{solve it} \Rightarrow \boxed{i_1 = 9A} \quad \boxed{i_2 = 2.5A} \quad \boxed{i_3 = 2A}$$

Therefore:

$$i_{R1} = -i_1 = -9A$$

$$i_{R2} = 7A$$

$$i_{R3} = i_2 - i_3 = (2.5 - 2)A = 0.5A$$

$$i_{R4} = i_2 = 2.5A$$

$$i_{R5} = i_3 = 2A.$$
